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# Effect of crystal-chemical growth conditions of single crystals of trigonal ferroborates $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ with huntite structure on their magnetic properties

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This work aimed to compare the magnetic properties of  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  single crystals grown from different solution melts: based on bismuth trimolybdate and lithium tungstate. Single crystals of this ferroborate from lithium-tungstate melt solution were grown for the first time. The chemical composition of ferroborates was determined using energy dispersive spectroscopy. It was found that  $\text{Bi}^{3+}$  ions replace  $\text{Nd}^{3+}$  ions ( $\sim 5\%$  at.) in the case of using bismuth trimolybdate solvent. When using a lithium-tungstate melt solution, impurities from the solvent do not enter the crystal matrix. From magnetic studies, the Neel temperatures  $T_N$  and paramagnetic Curie temperatures were determined, effective magnetic moments  $\mu_{\text{eff}}$  calculated, and phase diagrams of the magnetic state „temperature–magnetic field“ of the studied compounds were constructed.

**Keywords:** solution-melt method, magnetic dielectrics, antiferromagnets.

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## 1. Introduction

Rare-earth ferroborates with the structure of huntite  $R\text{Fe}_3(\text{BO}_3)_4$  ( $R = \text{Y}, \text{La}–\text{Lu}$ ) attract increased attention due to their unique physical properties. These compounds have a rhombohedral structure similar to the natural mineral huntite, described by space group  $R32$  or  $P3_121$ . The noncentrosymmetric structure makes these materials promising candidates for optical applications due to their good luminescence and nonlinear optical properties. For  $R\text{Fe}_3(\text{BO}_3)_4$  ferroborates it has been established that they belong to a new class of multiferroics, where magnetic, electrical, and elastic order parameters [1–7] coexist.

Magnetically, ferroborates are antiferromagnetic materials with two interacting magnetic subsystems (rare earth and iron subsystems). The iron subsystem is ordered at  $T_N = 30–40$  K. The rare-earth subsystem is magnetized by the  $f-d$  interaction and essentially contributes to the magnetic anisotropy and orientation of magnetic moments. I.e. the magnetic crystallographic anisotropy is determined specifically by the type of the rare-earth ion: either an easy-axis (EA) antiferromagnetic structure is implemented, when the spins of iron ions are ordered along the trigonal  $c$ -axis ( $R = \text{Dy}, \text{Tb}, \text{Pr}$ ) [2], or an easy-plane (EP) structure ( $R = \text{Nd}, \text{Sm}, \text{Eu}, \text{Er}, \text{Y}$ ) is implemented, when the spins of iron ions are ordered in the plane  $ab$  perpendicularly to  $c$ -axis of the crystal [2]. Besides, for ferroborates  $\text{GdFe}_3(\text{BO}_3)_4$  [8–10] and  $\text{HoFe}_3(\text{BO}_3)_4$  [3,11], when the temperature changes, a spin-flip transition is observed from the antiferromagnetic structure with anisotropy of „easy axis“ type to the structure of „easy plane“ type. A sim-

ilar transition is observed in the substituted ferroborate  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  [3,12].

It is important to note that anisotropy of rare-earth ions plays a major role in the magnetoelectric properties of rare-earth ferroborates. For example, for the easy-plane ferroborates of neodymium and samarium the electrical polarization arising in magnetic fields ( $\Delta P$ ), had the maximum value for the ferroborates and reached  $\sim 500 \mu\text{C}/\text{m}^2$  [2]. Induced by magnetic field  $\Delta P$  for ferroborates of europium and holmium ( $T > 5$  K), also having easy-plane anisotropy, reaches lower, but still substantial values of around dozens  $\mu\text{C}/\text{m}^2$  [3]. For highly anisotropic ions  $\text{Pr}^{3+}$ ,  $\text{Tb}^{3+}$ ,  $\text{Dy}^{3+}$  a magnetic structure of „easy-axis“ type is implemented, and the spins of ions  $\text{Fe}^{3+}$  are ordered below  $T_N$  along the trigonal  $c$ -axis of the crystal, which causes antiferromagnetic polarization of rare-earth ions due to  $f-d$  exchange. In this case the magnetoelectric effect has a much smaller value [2].

Initially, for isostructural nonlinear optical crystals of  $R\text{Fe}_3(\text{BO}_3)_4$  trigonal ferroborates, a technique was developed to grow them from melt solutions based on  $\text{K}_2\text{Mo}_3\text{O}_{10}–\text{B}_2\text{O}_3$  potassium trimolybdate [13]. Later, for growing single crystals of  $R\text{Al}_3(\text{BO}_3)_4$  and  $R\text{Fe}_3(\text{BO}_3)_4$  new melt solutions based on  $\text{Bi}_2\text{Mo}_3\text{O}_{12}–\text{B}_2\text{O}_3$  bismuth trimolybdate were proposed [14]. In these melt solutions,  $\text{Bi}_2\text{O}_3$  and  $\text{MoO}_3$  are bound stronger than  $\text{K}_2\text{O}_3$  and  $\text{MoO}_3$ . Therefore, the substitution of bismuth and molybdenum in the grown crystal for the rare-earth element was assumed to be relatively weak [15]. However, in some papers, the methods of chemical analysis, X-ray diffraction and magnetic studies were used to demonstrate that ions  $\text{Bi}^{3+}$  substitute the rare-earth ion in the quantity of  $\sim 5–6\%$  at., which

nevertheless is lower than the introduction of potassium and molybdenum [16–19]. In connection with the above, the lithium tungstate-based melt-solutions were proposed. It was assumed that ions from the solvent do not enter the crystal matrix in the latter case. Indeed, paper [17] shows, using the example of ferroborate  $\text{GdFe}_3(\text{BO}_3)_4$ , that this is truly the case.

This paper is dedicated to the comparison of the magnetic properties of mixed ferrobates  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ , grown from various solvents. For this purpose a technology of growth of the substituted ferrobate  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  was developed for the solution-melt on the basis of lithium tungstate  $\text{Li}_2\text{WO}_4\text{--B}_2\text{O}_3$ . Comparison was done to ferrobate  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ , grown from the solution-melt based on bismuth trimolybdate. It is important to note the special interest in this compound, since it was for it that a record value of magnetoelectric polarization was obtained in ferrobates ( $\sim 900 \mu\text{C}/\text{m}^2$ ) [3].

Ferrobate  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  at room temperature is described by the spatial group  $R32$ , and at low temperatures  $P3_121$  [20]. The magnetic structure is not yet known for certain. Theoretical calculations, as a possible option, suggest the presence of the angular phase below the temperature of the spin-flip transition [12].

## 2. Experimental techniques and sample preparation

Single crystals of ferrobate  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  were grown from two solution-melt systems: based on bismuth trimolybdate  $\text{Bi}_2\text{Mo}_3\text{O}_{12}\text{--B}_2\text{O}_3$ , described in detail in paper [12] and on the basis of lithium tungstate  $\text{Li}_2\text{WO}_4\text{--B}_2\text{O}_3$ . In the last case the ferrobates  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  were grown for the first time. For this purpose a technology was developed for growth from the solution-melt to a seed.

The following solution-melt was selected to grow crystals  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ :

80 % wt.  $\{\text{Bi}_2\text{Mo}_3\text{O}_{12} + 3\text{B}_2\text{O}_3 + 0.5(\text{Nd}_2\text{O}_3 + \text{Ho}_2\text{O}_3)\}$   
+ 20 % wt.  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ .

The following were melted to prepare 100 g of solution-melt:

$\text{B}_2\text{O}_3$ –16.2 g,  $\text{Bi}_2\text{O}_3$ –25.6 g,  $\text{MoO}_3$ –24.0 g,  $\text{Fe}_2\text{O}_3$ –8.6 g,  $\text{Nd}_2\text{O}_3$ –11.82 g,  $\text{Ho}_2\text{O}_3$ –13.78 g.

The second solution-melt:

78 % wt.  $\{\text{Li}_2\text{WO}_4 + 3.3\text{B}_2\text{O}_3 + 0.5(\text{Nd}_2\text{O}_3 + \text{Ho}_2\text{O}_3)\}$   
+ 22 % wt.  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  ( $\text{Li}_2\text{WO}_4$ –24.05 g,  $\text{B}_2\text{O}_3$ –26.62 g,  $\text{Ho}_2\text{O}_3$ –21.09 g,  $\text{Nd}_2\text{O}_3$ –18.78 g,  $\text{Fe}_2\text{O}_3$ –9.45 g).

Areas of stability of  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  crystals are defined by the method of direct phase probing.

The same method was used to grow for both types of solution-melts. Solution-melts were prepared in a platinum cylindrical crucible ( $D = 57 \text{ mm}$ ,  $H = 65 \text{ mm}$ ) by subsequent fusion of oxides  $\text{B}_2\text{O}_3 + [\text{Bi}_2\text{O}_3 + \text{MoO}_3$  or  $\text{Li}_2\text{WO}_4]$ ,  $[\text{Nd}_2\text{O}_3 + \text{Ho}_2\text{O}_3 + \text{Fe}_2\text{O}_3]$  at  $T = 1050\text{--}1100^\circ\text{C}$ . Then the crucible with the prepared solution-melt was

placed into a crystallization furnace. The solution-melt was homogenized at  $T = 1000^\circ\text{C}$  for 5–10 h with a rod-shaped crystal holder immersed in it and rotating with the speed of  $\omega = 1 \text{ rps}$ . The preliminary search for the saturation temperature ( $T_{\text{sat}}$ ) was carried out via observations of spontaneous crystals formed on the crystal holder. After repeated homogenization  $T_{\text{sat}}$  was confirmed within  $\pm 2^\circ\text{C}$  using the crystals that were already obtained. Usually 4 „point“ seeds were fixed on the rod-shaped crystal holder, which were high quality crystals with the linear size  $\sim 1 \text{ mm}$ .

The saturation temperature was  $960^\circ\text{C}$  for the first and  $980^\circ\text{C}$  for the second solution-melt. The width of the metastable area  $\Delta T_{\text{met}} \approx 12^\circ\text{C}$  was determined as the maximum supercooling with no spontaneous nucleation for 20 h.

After reheating of the solution-melt at  $T = 1000^\circ\text{C}$  for 2–4 h the crystal holder with the seeds was suspended above the solution-melt, and the temperature in the furnace decreased down to  $T = T_{\text{sat}} + 7^\circ\text{C}$ .

After 15 minutes the crystal holder was immersed into the solution-melt for the depth of 15–20 mm, and reversible rotation (with the period of 1 min) with the speed of  $\omega = 1 \text{ rps}$  was activated. In  $t = 15 \text{ min}$ . the temperature decreased down to the start  $T = T_{\text{sat}} - 7^\circ\text{C}$ , which corresponds to the middle of the metastable zone. Further the temperature of the solution-melt decreased gradually according to the program with the increasing rate  $1\text{--}2^\circ\text{C}/\text{day}$ , calculated at the crystal growth speed of not more than 1 mm/day.

After the growth process was completed, the crystal holder was raised above the solution-melt and cooled down to room temperature with the furnace power supply off. The solution-melts for the 30-day cycle usually lost by evaporation not more than 2 % wt. After supplementation with the crystal-forming oxides in the quantity corresponding to the mass of the extracted crystals, they had  $T_{\text{sat}}$  close to the initial ones and were reused. The crystals were freed from the remains of the solution-melt by etching in a hot 20 % aqueous solution of nitric acid.

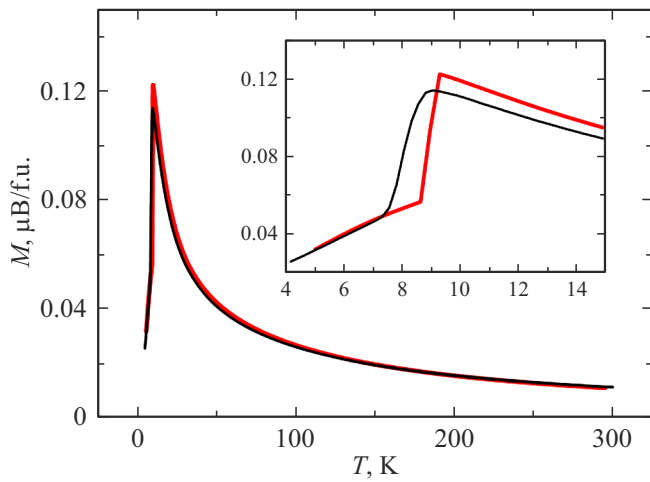
The magnetic properties were studied on a PPMS-9 (Quantum Design) vibration magnetometer in the in the temperature range of 4.2–300 K and magnetic fields of up to 9 T.

The chemical composition of the grown crystals was studied by the method of energy-dispersive spectroscopy (EDX) using a Bruker XFlash 430-H (Germany) detector connected to an electronic microscope. The studied crystals were attached to a metal table with the help of a two-sided conducting carbon scotch tape. Then the table with the attached samples was placed into a work chamber of a scanning electron microscope Hitachi SU3500 (Japan). To obtain the electronic microphotographs, accelerating voltage 20 kV was specified. Observation was carried out in the mode of back-scattered electrons (BSE), since in this mode the signal of reflected electrons was sensitive to the composition contrast. For each sample the parts

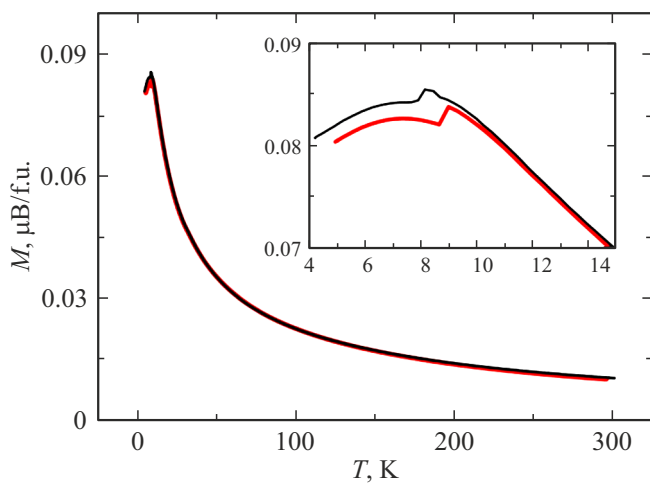
were selected for elemental mapping and semi-quantitative analysis of the chemical composition.

### 3. Experimental results

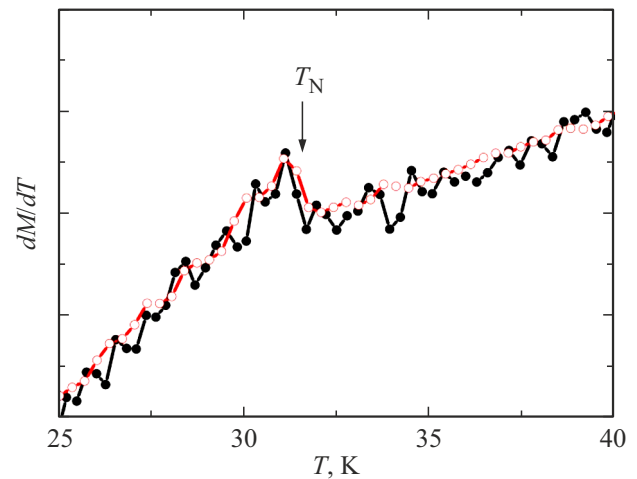
Figures 1 and 2 present the temperature dependences of magnetization of compounds  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{Bi}$  (grown from trimolybdate bismuth solution-melt) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (grown from tungstate lithium solution-melt) with the magnetic field orientation along (Figure 1) and perpendicularly to the triad axis of  $c$ -axis (Figure 2). From the charts you can see that at high temperatures the magnetization increases according to the Curie–Weiss law.



**Figure 1.** Temperature dependences of magnetization of compounds  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{Bi}$  (black) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (red), measured in the magnetic field  $H = 1 \text{ kOe}$ , in the  $H \parallel c$  geometry. The insert shows the same in a different scale.



**Figure 2.** Temperature dependences of magnetization of compounds  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{Bi}$  (black) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (red), measured in the magnetic field  $H = 1 \text{ kOe}$ , in the  $H \perp c$  geometry. The insert shows the same in a different scale.



**Figure 3.** Temperature dependence  $dM/dT$  for  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{Bi}$  (black) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (red).

In the area of  $\sim 30 \text{ K}$  there is a light fracture corresponding to the temperature of the antiferromagnetic ordering of the iron subsystem  $T_N$ . This transition is seen best on the derivative of the magnetization by temperature (Figure 3). You can see that Néel temperatures  $T_N$  of samples are practically the same and are equal to  $T_N = 31.5 \text{ K}$ . This once again indicates that the long-range magnetic order in ferroborates firstly depends on the subsystem of iron ions  $\text{Fe}^{3+}$ .

Further, as the temperature decreases in the area of  $8\text{--}9 \text{ K}$ , both directions of the magnetic field  $H \parallel c$  and  $H \perp c$  on dependences  $M(T)$  demonstrate a drastic fracture. This feature was interpreted previously as a spin-flip transition from the state of „easy plane“ (EP) type to the state of „easy axis“ (EA) type [3]. In reality the situation is much more complicated, since there might also be an angular phase in a certain temperature and magnetic field range, and also noncollinear magnetic sublattices [12]. Such transition is observed in  $\text{HoFe}_3(\text{BO}_3)_4$  as well, where it is also impossible to correctly reduce the considered antiferromagnetic structure to the classic two-sublattice model.

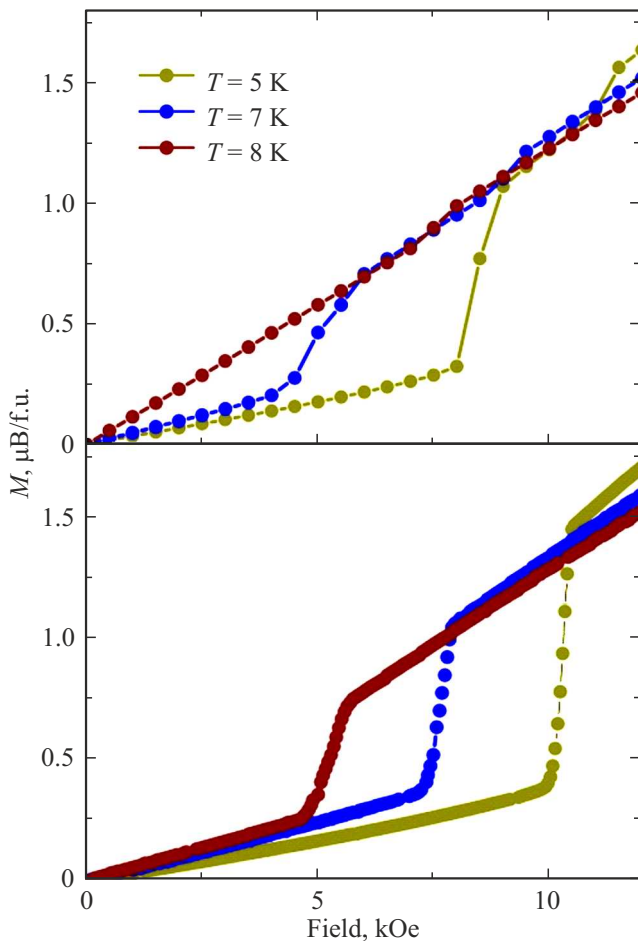
From the dependences  $M(T)$  you can see that the temperature of the spin-flip transition ( $T_{SR}$ ) is approximately  $1^\circ \text{ K}$  higher in  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ , then in  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{Bi}$ .

Figures 4 and 5 show the field dependences of magnetization at the various temperatures measured in the orientation of the magnetic field along and perpendicularly to the  $c$ -axis of the crystal. You can see that the spin-flip transition is observed for both magnetic field directions:  $H \parallel c$  and  $H \perp c$ . Note that in  $H \parallel c$  direction the field dependences correspond to the behavior of the two-sublattice antiferromagnetic (Figure 4). In case of magnetic field orientation perpendicularly to the  $c$ -axis of the crystal, the considered magnetic structure may not be reduced to the

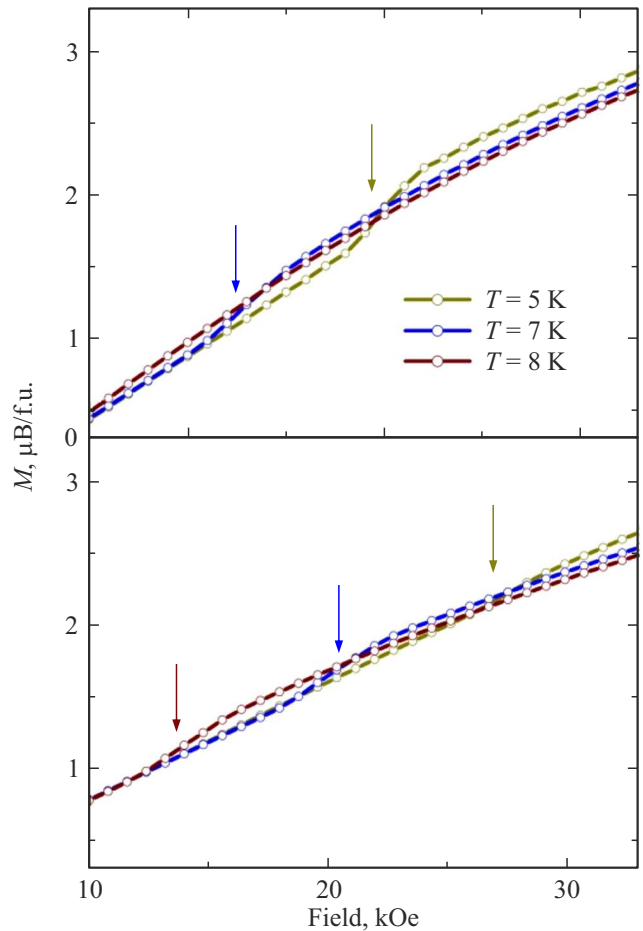
collinear two-sublattice model (Figure 5). Since in case of  $H \perp c$  no features must be observed, the field dependence  $M(H)$  must be linear. Despite the above results, we will continue so far to interpret the observed spin-flip transition as the transition of „easy plane“–„easy axis“ type.

From Figures 4 and 5 you can see that as the temperature increases, the critical field of the spin-flip transition ( $H_{SR}$ ) moves to the area of small fields and is not observed at all above a certain temperature. Comparing  $M(H)$  for this two compounds, you may note that  $H_{SR}$  for  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{:Bi}$  is lower by value than  $H_{SR}$  for  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  for both orientations of the magnetic field  $H \parallel c$  (Figure 4) and  $H \perp c$  (Figure 5).

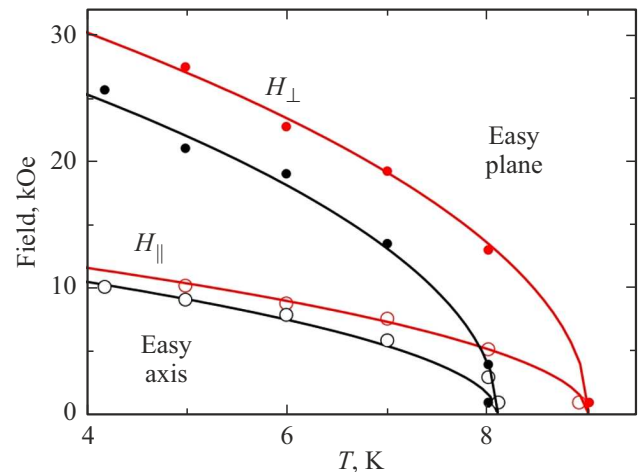
Temperature dependences of the critical fields of transitions between the EA and EP states for both compositions and orientations of the magnetic field  $H \parallel c$  and  $H \perp c$  are built using  $M(T)$  and  $M(H)$  data. In Figure 6, where these dependences are presented, magnetic phase diagrams  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{:Bi}$  and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  are shown in the corresponding magnetic fields. EA and EP states are located above and below the corresponding phase boundary.



**Figure 4.** Field dependences of magnetization of compounds  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{:Bi}$  (top) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (bottom), measured at different temperatures in the  $H \parallel c$  geometry.



**Figure 5.** Field dependences of magnetization of compounds  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{:Bi}$  (top) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (bottom), measured at different temperatures in the  $H \perp c$  geometry.



**Figure 6.** The magnetic phase diagram for  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{:Bi}$  (black) and  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (red) in the magnetic field applied in parallel and perpendicularly to the  $c$ -axis of the crystal.

From the diagrams you can see that the value of the spin-flip transition is higher for  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ , than for  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4\text{:Bi}$  in the entire  $(T-H)$  space.

Magnetic parameters of the studied compounds

	Ho <sub>0.5</sub> Nd <sub>0.5</sub> Fe <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub> :Bi	Ho <sub>0.5</sub> Nd <sub>0.5</sub> Fe <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>
Confirmed composition	Ho <sub>0.50</sub> Nd <sub>0.45</sub> Bi <sub>0.05</sub> Fe <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>	Ho <sub>0.42</sub> Nd <sub>0.58</sub> Fe <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>
$T_N$ , K	31.5	31.5
$\theta_{  }$ , K	-55.1	-38.5
$\theta_{\perp}$ , K	-80.4	-66.1
$\mu_{\text{eff}}$ , $\mu_B$	13.3	12.8
$\mu_{\text{theor}}$ , $\mu_B$	12.95	12.73

#### 4. Discussion of results

In the paramagnetic area for both compositions the magnetization is ruled by Curie-Weiss law, where you can find the paramagnetic Curie  $\theta$  temperatures and effective magnetic torque  $\mu_{\text{eff}}$ . Experimentally found  $\theta$  depend both on the composition and the direction of the magnetic field (see table). The negative sign  $\theta$  indicates the presence of antiferromagnetic exchange interaction in the magnetic system, which is typical for all ferroborates with the huntite structure. You can see that the value  $\theta$  has a lower value (by absolute value) in Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>, vs. Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:Bi. This fact was a surprise. It seemed it had to be the other way round, since non-magnetic bismuth ions Bi<sup>3+</sup> had to substitute magnetic ions Nd<sup>3+</sup> and Ho<sup>3+</sup>.

The experimentally determined effective magnetic torque of one structural unit  $\mu_{\text{eff}}$  was calculated from the tangent of inclination of the inverse dependence of temperature dependence of magnetic susceptibility  $\chi^{-1}(T)$  and is presented in the table. It turned out that the effective magnetic torque in compound Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:Bi is higher by 0.5  $\mu_B$  than in Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>, even though it had to be the other way round here as well.

The theoretical value of the effective magnetic torque may be calculated as follows:

$$\mu_{\text{theor}} = \sqrt{3 \cdot g_S^2 \cdot \langle S_{\text{Fe}} \rangle^2 \cdot \mu_B^2 + n_1 \cdot g_{J\text{Ho}}^2 \cdot \langle J_{\text{Ho}} \rangle^2 \cdot \mu_B^2 + n_2 \cdot g_{J\text{Nd}}^2 \cdot \langle J_{\text{Nd}} \rangle^2 \cdot \mu_B^2}, \quad (1)$$

where  $g_S = 2$  —  $g$ -factor accounting for only the spin magnetic torque,  $g_{J\text{Ho}} = 5/4$  — Landé factor for ion Ho<sup>3+</sup>,  $g_{J\text{Nd}} = 8/11$  — Landé factor for ion Nd<sup>3+</sup>,  $\langle S_{\text{Fe}} \rangle^2 = S \cdot (S + 1)$  — square of operator of iron ion spin moment ( $S = 5/2$  for Fe<sup>3+</sup>),  $\langle S_{\text{Ho}} \rangle^2 = J \cdot (J + 1)$  — square of operator of holmium ion full moment ( $J = 8$  for Ho<sup>3+</sup>),  $\langle S_{\text{Nd}} \rangle^2 = J \cdot (J + 1)$  — square of operator of neodymium ion full moment ( $J = 8$  for Nd<sup>3+</sup>),  $n_1$ ,  $n_2$  — share of holmium and neodymium ions, accordingly ( $n_1 + n_2 = 1$ ).

If the ideal case is suggested that holmium and neodymium ions enter the crystal matrix at the ratio of 1:1, and there are no impurities, in this case the theoretical value of  $\mu_{\text{eff}}$  will be equal to 12.95  $\mu_B$ . This value is close to the

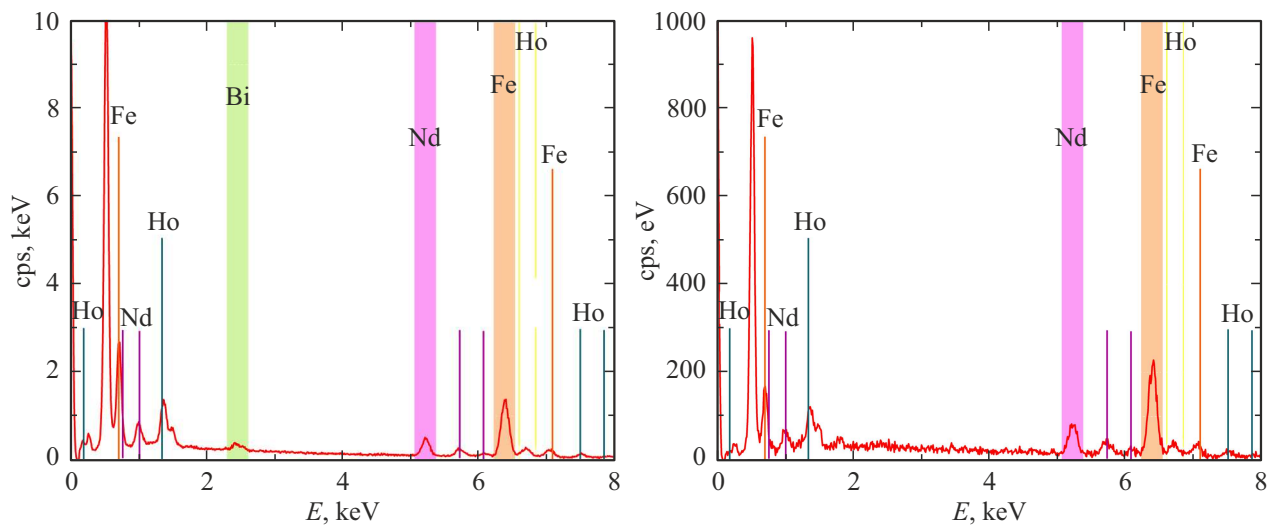
experimentally defined values  $\mu_{\text{eff}}$  for Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> and Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:Bi. However, a question arises — why  $\mu_{\text{eff}}$  for Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> is below the theoretical one, and for Ho<sub>0.5</sub>Nd<sub>0.5</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:Bi it is higher?

Therefore, to understand a fuller picture, the EDX method was used in an attempt to define the chemical composition of the studied compounds. The compositions of both compounds were defined based on the analysis of X-ray fluorescence spectra in Figure 7. Use of Quantax Espirit software suite yields the following calculation results: Ho<sub>0.50</sub>Nd<sub>0.45</sub>Bi<sub>0.05</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> — for the sample grown from bismuth trimolybdate solution-melt and Ho<sub>0.42</sub>Nd<sub>0.58</sub>Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> — for the sample grown from lithium tungstate solution-melt. It should be noted that the relative error in the composition definition was  $\delta = 1.5\%$ .

Such different content of Ho<sup>3+</sup> and Nd<sup>3+</sup> ions in ferroborates may be explained as follows. As is known, when crystals are made from bismuth molybdate solution-melt, partial substitution occurs in the rare earth subsystem. Besides, taking into account the fact that the ionic radius of neodymium Nd<sup>3+</sup> is closer to the ionic radius of bismuth Bi<sup>3+</sup> (98.3 and 120 pm, respectively), and a substantially larger difference with the ionic radius of holmium (90 pm), substitution mostly happens in the neodymium subsystem.

For the lithium tungstate system there can be no such substitution, since ionic radii of lithium and tungsten (73 pm and 62 pm, respectively) differ substantially from ionic radii of rare earths. Here, probably, the coefficients of distribution among the crystal and the solution-melt are slightly higher than one for neodymium and lower for holmium. In this case the distribution coefficient may not be calculated in advance, but may only be selected using experimental data.

For understanding of the entire picture of magnetic behavior, it is necessary to take into account all competing exchange interactions in this compound [12]. As it is known, magnetic torques of iron ions Fe<sup>3+</sup> in HoFe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> are antiferromagnetically ordered at  $T_N \sim 38-39$  K, and when temperature lowers down to  $T_{SR}$ , some of them lie in the basal plane  $ab$ , as well as all magnetic torques of Ho<sup>3+</sup> ions, and other Fe<sup>3+</sup> ions are arranged at the angle to the plane [21]. At  $T_{SR} = 4.7$  K the spontaneous spin-flip transition occurs, as a result of which the magnetic torques of holmium are arranged at the angle to the third order



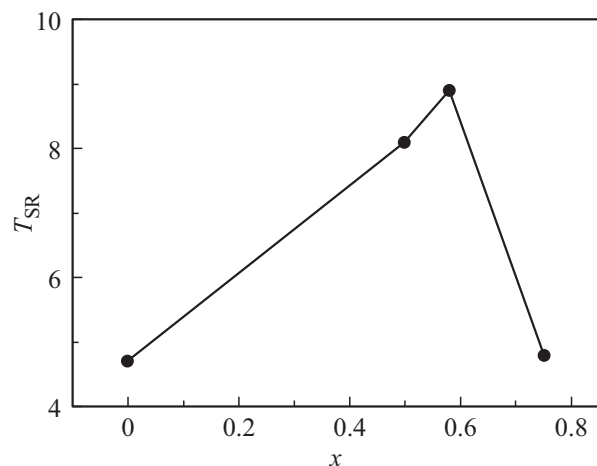
**Figure 7.** Spectrum of X-ray radiation from samples  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$ , grown using bismuth trimolybdate (left) and lithium tungstate (right) solution-melts.

axis, while the Fe-subsystem becomes oriented along the  $c$ -axes. In  $\text{NdFe}_3(\text{BO}_3)_4$  at  $T < T_N \sim 31$  K all magnetic torques are in the basal plane  $ab$  [22]. Therefore, as a result of competition of different contributions from Ho-, Nd- and Fe-subsystems to the magnetic anisotropy, spontaneous and magnetic field induced spin-flip transitions may arise in  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  compound.

Such transitions were detected for  $x = 0.5$  [3,12] and 0.75 [23] compositions. It seemed evident that substitution of  $\text{Ho}^{3+}$  ions for  $\text{Nd}^{3+}$  ions that stabilized the easy plane state in  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  should have resulted in the temperature shift of the spin-flip transition from the EP type state to EA state from the value detected in  $\text{HoFe}_3(\text{BO}_3)_4$  ( $T_{SR} = 4.7$  K) to the area of lower temperatures. However, in  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  temperature  $T_{SR}$  suddenly increased to 8 K [3], and in  $\text{Ho}_{0.25}\text{Nd}_{0.75}\text{Fe}_3(\text{BO}_3)_4$  the value  $T_{SR}$  remained approximately the same as in  $\text{HoFe}_3(\text{BO}_3)_4$  [23]. This result clearly shows that simple summation of contributions from EA- and EP-subsystems in the substituted compound is not enough to explain the processes happening in the resulting magnetic structure. Thus, paper [12] shows that increase of  $T_{SR}$  in  $\text{Ho}_{0.5}\text{Nd}_{0.5}\text{Fe}_3(\text{BO}_3)_4$  (compared to  $\text{HoFe}_3(\text{BO}_3)_4$ ) is caused by expansion of the temperature range of the initial low-temperature state of the magnetic subsystem as a result of its change from the easy axis state (as in  $\text{HoFe}_3(\text{BO}_3)_4$ ) to the angular state.

Therefore, it is evident that the temperature of spin-flip transition in  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$ , first of all depends on holmium ion  $\text{Ho}^{3+}$ , besides, this contribution is non-linear and depends on its content in  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$ .

Figure 8 shows the dependence of temperature  $T_{SR}$ , determined in the magnetic field 1 kOe, on the content of  $\text{Ho}^{3+}$  ions in the  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  compound. You can see that as concentration  $x$  increases, temperature  $T_{SR}$  grows



**Figure 8.** Dependence of temperature of spin-flip transition  $T_{SR}$  in  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  on concentration  $x$ . The data for  $x = 0$  is taken from paper [11], for  $x = 0.75$  from paper [23], others — from the presented paper.

first, reaches its maximum in the range of  $x = 0.58$ – $0.75$ , and only after the maximum value is achieved, it starts decreasing.

However, it should be noted that you should not reduce everything to the impact of  $\text{Ho}^{3+}$  ions. In paper [12] within the single theoretical approach based on the approximation of the molecular field and calculations in the model of the crystalline field for a rare-earth ion it was shown that this spin-flip transition is caused by various temperature dependences of the competing contributions of rare-earth (Ho and Nd) and Fe-subsystems to the full magnetic anisotropy  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$ . Therefore, for more complete understanding of the observed magnetic behavior it is further necessary to additionally study the diffraction of neutron elastic scattering.

## 5. Conclusion

For the first time  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  single crystals were grown from the lithium tungstate solution-melt (with  $x = 0.5$  for charging). For the purpose of comparison,  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  single crystals ( $x = 0.5$  for charging) were grown with the use of a solvent based on bismuth trimolybdate. A comparative analysis of magnetic properties of the grown ferroborates was carried out.

The EDX method was used to determine the chemical composition of ferroborate:  $\text{Ho}_{0.50}\text{Nd}_{0.45}\text{Bi}_{0.05}\text{Fe}_3(\text{BO}_3)_4$  — for the sample grown from bismuth trimolybdate solution-melt and  $\text{Ho}_{0.42}\text{Nd}_{0.58}\text{Fe}_3(\text{BO}_3)_4$  — for the sample grown from lithium tungstate solution-melt. It was shown that  $\text{Bi}^{3+}$  ions mostly substitute neodymium ions  $\text{Nd}^{3+}$ , if the growth is carried out from the bismuth trimolybdate solution-melt. In case of use of lithium tungstate solvent, neither lithium ions, nor tungsten ions enter the crystal matrix. However, it turned out that the coefficients of distribution among the crystal and the solution-melt are slightly higher than one for neodymium and lower for holmium. It is related to the fact that the distribution coefficient may not be calculated in advance, but may only be selected using experimental data.

The magnetic studies identified the Néel temperatures, paramagnetic Curie temperatures, effective magnetic torques  $\mu_{\text{eff}}$  were calculated. In both cases  $\mu_{\text{eff}}$  turned out to be slightly higher than the one calculated theoretically, with account of the chemical composition for these compounds. „Temperature–magnetic field“ phase diagrams of the magnetic state for the crystals under study are plotted.

It was shown that the shift of the spin-flip transition  $T_{SR}$  in  $\text{Ho}_{0.42}\text{Nd}_{0.58}\text{Fe}_3(\text{BO}_3)_4$  in the area of higher temperatures and fields, compared to  $\text{Ho}_{0.50}\text{Nd}_{0.45}\text{Bi}_{0.05}\text{Fe}_3(\text{BO}_3)_4$  complies with the representation that the concentration of  $\text{Ho}^{3+}$  ions in  $\text{Ho}_{1-x}\text{Nd}_x\text{Fe}_3(\text{BO}_3)_4$  impacts non-linearly by the value  $T_{SR}$  with a pronounced maximum in the range of  $x = 0.58–0.75$ . For complete understanding of magnetic behavior further research of neutron elastic scattering diffraction is necessary.

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## Conflict of interest

The authors declare that they have no conflict of interest.

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