## <sup>13,01</sup> Electron-phonon interaction in the surface dimer adsorption model

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In the scope of the model of surface dimer, formed by the adsorbed atom and below lying substrate surface atom, the problem on the electron-phonon interaction effect on the charge transfer in adsorbed system is considered. The case of adsorption on metal is examined thor oughly.

Keywords: adsorbate, substrate, dimer's vibrations, charge transfer.

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## 1. Introduction

To the best of the authors' knowledge, the question of the adatom vibrations effect on its electronic state was first considered in articles [1-3]. In this case, the adsorption standard model (ASM) was used on Anderson-Newns metals [4,5]. Recently, to describe adsorption on solid substrates, the surface dimer model (SDM) was proposed, which, unlike the standard model, considers not an adsorbed particle, but a surface molecule formed by this particle and the nearest atom of the substrate surface [6]. In this article, we consider how vibrations of a surface dimer affect the electronic characteristics of an adsorption system and, most importantly, charge transfer within a dimer and between a dimer and a substrate. Although in the case under consideration it is more correct to speak of electron-vibrational interaction, we will use the standard term "electron-phonon" interaction, comparing the eigenfrequency of  $\Omega$  dimer vibrations with a phonon with a zero wave vector.

Let us represent the Hamiltonian of a free (not bound to the substrate) dimer  $H_{\rm dim}$ , consisting of atoms *a* (adsorbed atom) and *s* (surface atom of the substrate), which orbitals are characterized by energies  $\varepsilon_a$  and  $\varepsilon_s$ , and the occupation numbers are 1, as the sum of  $H_{\rm dim} = H_{el} + H_{vib} + H_{\rm int}$ . The Hamiltonian of the subsystem of spinless electrons has the form

$$H_{el} = \varepsilon_a \hat{n}_a + \varepsilon_s \hat{n}_s - t(s^+a + a^+s), \tag{1}$$

where *t* is energy of electron hopping between atoms *a* and *s*,  $\hat{n}_a = a^+a$  and  $\hat{n}_s = s^+s$  are atomic number operators for *a* and *s*,  $a^+(a)$  and  $s^+(s)$  are electron creation (annihilation) operators,  $n_{s(a)}$  are atomic occupation numbers *a* and *s* [6]. The Hamiltonian  $H_{vib}$  describing the vibrations of a free surface dimer can be represented in the classical form

$$H_{vib} = \frac{1}{2}Ml^2 + \frac{1}{2}k(l-l_0)^2,$$
 (2)

where *M* is reduced mass of dimer atoms,  $k = M\Omega^2$  is force constant of dimer with equilibrium length  $l_0$ . The Hamiltonian of the interaction  $H_{int}$  between the electronic and vibrational subsystems of a free dimer is

$$H_{\rm int} = \nu (\hat{n}_a + \hat{n}_s)(l - l_0), \tag{3}$$

where  $\nu$  is deformation constant of the surface dimer. Using the relation  $\partial \langle H_{\text{dim}} \rangle / \partial l = \langle \partial H_{\text{dim}} / \partial l \rangle$ , we get  $l - l_0 = -\nu (n_a + n_s)/k$ . Then the Hamiltonian  $H_{\text{dim}}$  can be written as

$$H_{\rm dim} = w_a \hat{n}_a + w_s \hat{n}_s - t(s^+ a + a^+ s) + H'.$$
(4)

Here  $w_{a(s)} = \varepsilon_{a(s)} - \lambda n_{a(s)}$ , where  $\lambda = \nu^2/k$  is the constant of the electron-phonon interaction of the surface dimer and the term H' contains all the contributions that do not have an operator structure. Using the results of [6] and neglecting the metallicity of the bond, we obtain

$$\nu = (\partial \sqrt{t^2 + \delta^2}/\partial l)_{l=l_0} = 4t\alpha_c/l_0,$$
  
$$k = 4\alpha_c t (1 - 2\alpha_p^2)/l_0^2 \text{ and } \lambda = 4\alpha_c t/(1 - 2\alpha_p^2),$$

where bond covalency  $\alpha_c = t/\sqrt{t^2 + \delta^2}$ , bond polarity  $\alpha_p = \sqrt{1 - \alpha_c^2}$  and  $\delta = (\varepsilon_a - \varepsilon_s)/2$  [7].

Hamiltonian (4) corresponds to the Green's function of the free dimer  $g_{\dim}^{\pm}(\omega) = (\omega - \omega_{\pm} + i0^{+})^{-1}$ , where  $\omega$  is energy variable and energies of local levels are  $\omega_{\pm} = w \pm R$ ,  $R = \sqrt{\Delta^{2} + t^{2}}$ ,  $w = (w_{a} + w_{s})/2$  and  $\Delta = (w_{a} - w_{s})/2$ . The densities of atom states of a free dimer are

$$\rho_{a,s}(\omega) = D_{\pm}\delta(\omega - \omega_{+}) + D_{\mp}\delta(\omega - \omega_{-}),$$

where  $D_{\pm} = (1 \pm \Delta/R)/2$  (upper signs refer to atom *a*, lower refer to atom *s*),  $\delta(\ldots)$  is Dirac delta function. The state density of the free dimer itself is  $\rho_{\dim}(\omega) = \delta(\omega - \omega_+) + \delta(\omega - \omega_-)$ , and the occupation number  $n_{\text{dim}} = 2[\Theta(\omega - \omega_+) + \Theta(\omega - \omega_-)]$ , where  $\Theta(\ldots)$  is Heaviside function. Then, we set  $\varepsilon_a + \varepsilon_s - 2\lambda = 0$ , where we take into account that  $n_a + n_s = 2$  in a free dimer. The charge transfer between atoms of a free dimer is  $m = n_a - n_s$ , so  $\Delta = \delta - \lambda m/2$ , where  $\delta = (\varepsilon_a - \varepsilon_s)/2$ . It is easy to show that  $\partial m/\partial \lambda = -mt^2/R^3$ , i.e. as  $\lambda$  increases, the value of |m|decreases.

Let's take into account the presence of a substrate. In the weak coupling limit ( $\Gamma(\omega) \ll t$ ), dencity of states of the epitaxial dimer densities of the epitaxial dimer (epidimer)  $\bar{\rho}_{dim}(\omega)$  and its constituent atoms  $\bar{\rho}_{a(s)}(\omega)$  can be represented as

$$\bar{\rho}_{a(s)}(\omega) = D_{\pm}\rho_{+}(\omega) + D_{\mp}\rho_{-}(\omega),$$
$$\bar{\rho}_{\dim}(\omega) = \rho_{+}(\omega) + \rho_{-}(\omega),$$
$$\rho_{\pm}(\omega) = \frac{1}{\pi} \frac{\Gamma(\omega)}{(\omega - \omega_{\pm} - \Lambda(\omega))^{2} + \Gamma^{2}(\omega)}.$$
(5)

Here  $\Gamma(\omega) = \pi V^2 \rho_{sub}(\omega)$  is the local level broadening function  $\omega_{\pm}$ , the function

$$\Lambda(\omega) = V^2 P \int_{-\infty}^{\infty} \rho_{\rm sub}(\omega')(\omega - \omega') d\omega'$$

determines the shift of these levels,  $\rho_{sub}(\omega)$  is density of substrate states, V is matrix element of the interaction of  $\omega_{\pm}$  levels with substrate states, P is principal value symbol. For further analysis, it is necessary to specify the substrate by setting the function  $\rho_{sub}(\omega)$ .

Let us consider adsorption on metal. Setting  $\rho_{\text{sub}}(\omega) = \rho_m = \text{const}$  (Anderson model [5]), we find  $\Gamma(\omega) = \Gamma_m = \pi V^2 \rho_m$  and  $\Lambda(\omega) = \Lambda_m = 0$ . Then the densities of states of the epidimer atoms  $\bar{\rho}_{a(s)}^m(\omega)$  are the sums of two Lorentz profiles  $\rho_{\pm}^m(\omega) = \Gamma_m / \pi [(\omega - \omega_{\pm})^2 + \Gamma_m^2]$  with weight factors  $D_{\pm}$  [6,7]. At zero temperature, the level occupation numbers  $\omega_{\pm}$  are equal to

$$n_{\pm}^{m}=2\int_{-\infty}^{\varepsilon_{F}}
ho_{\pm}^{m}(\omega)d\omega,$$

where  $\varepsilon_F$  is the Fermi level of the system, whence, taking into account (5), we find  $n_{\pm}^m = (2/\pi) \operatorname{arccot}[(\omega_{\pm} - \varepsilon_F)/\Gamma_m]$ . For the epidimer, the occupation number is

$$\bar{n}_{\dim}^m = n_+^m + n_-^m$$
 and  $\bar{m}^m \equiv \bar{n}_a^m - \bar{n}_s^m = (\bar{\Delta}/\bar{R})(n_+^m - n_-^m)$ 

where  $\bar{\Delta} = \delta - \lambda \bar{m}^m/2$ ,  $\bar{R} = \sqrt{\bar{\Delta}^2 + t^2}$ . At  $\varepsilon_F = 0$  there is no charge transfer between the dimer and the substrate, so  $\bar{n}_{dim}^m = 2$ . The interatomic charge transfer inside the dimer is

$$\bar{m}^m = (2\bar{\Delta}/\pi\bar{R}) \left[ \arctan(\omega_-/\Gamma_m) - \arctan(\omega_+/\Gamma_m) \right].$$

In the weak coupling regime, the dimer-substrate  $\Gamma_m/|\omega_{\pm}| \ll 1$  and  $\Gamma_m/R \ll 1$  in the first approximation, we have

$$n^m_+(\varepsilon_F=0) \approx 2\Gamma_m/\pi\omega_+$$
 and  $n^m_-(\varepsilon_F=0) \approx 2 - 2\Gamma_m/\pi\omega_-$ 

Therefore,

$$(ar{m}^m)_{arepsilon_F=0}pprox -2(ar{\Delta}/ar{R})(1-2\Gamma_m/\piar{R}).$$

Thus, at  $\varepsilon_F = 0$ , the value of the interatomic charge transfer in the epidemer is smaller than in the free dimer. In the limit  $|\varepsilon_F| \ll |\omega_{\pm}|$  we have  $n_{\pm}^m \approx n_{\pm}^m (\varepsilon_F = 0) - 2\rho_{\pm}^m (\omega_{\pm})\varepsilon_F$ , where  $\rho_{\pm}^m (\omega_{\pm})\varepsilon_F \sim \Gamma_m \varepsilon_F / \bar{R}^2$ , i.e. it is a quantity of the second order infinitesimal. In the same limit, the charge transfer between the dimer and the substrate is  $\bar{m}_{\dim}^m = 2 - \bar{n}_{\dim}^m \approx 2\Gamma_m / \bar{R}$ , or a quantity of the first order infinitesimal. At the same time  $\partial \bar{m}_{\dim}^m / \partial \lambda = (\Gamma_m \bar{\Delta} / \bar{R}^3) \bar{m}_{\dim}^m$ , so that the electron-phonon interaction increases the value of  $|\bar{m}_{\dim}^m|$  at  $\bar{\Delta} > 0$  and decreases it at  $\bar{\Delta} < 0$ .

Above, we considered the case of a weak bond between the dimer and the substrate. It is easy to show (e.g. see [8]) that in the strong bond regime in the zeroth order in  $t^2/\Gamma_m^2$ the problem of epidimer is reduced to the problem of adsorption of two isolated atoms *a* and *s*. If, as in the article [8], we take into account the Coulomb repulsion *G* of electrons of atoms *a* and *s*, then expression (4) will be valid after replacing  $w_{a(s)} = \varepsilon_{a(s)} - \lambda n_{a(s)}$  with  $w'_{a(s)} = \varepsilon_{a(s)} + Gn'_{s,a} - \lambda n'_{a(s)}$ .

In this article, we considered adsorption on a metal with a constant state density (Anderson model), which is applicable to the description of simple (non-transitional) metals with a wide *sp*-band. For *d*- and *f*-metals, it is more correct to use the Friedel state density model of "pedestal" type [9], shift function  $\Lambda(\omega)$  for which is given in [10]. Note that the Friedel model is also suitable for describing two-dimensional metals [11]. In case of adsorption on semiconductor and dielectric substrates, it is convenient to use the Haldane–Anderson state density model [5,12]. Adsorption on graphene-like compounds is considered in [13].

Unfortunately, it should be noted that the question of the role of the electron-phonon interaction in adsorption has not been practically studied (e.g. see [4,14]), although, on the other hand, there is growing interest in electron-phonon effects in epitaxial [15,16] and free [17-19] two-dimensional layers and topological insulators [20,21]. Therefore, in the adsorption problem, due to the lack of information, we used the simplest model of electron-phonon interaction, similar to the widely used one-phonon Holstein model [22,23].

## **Conflict of interest**

The authors declare that they have no conflict of interest.

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